1.	The distribution of populations in a group of counties is shown in this pie chart. What percent of the counties have fewer than 100,000 residents? Distribution of County Populations $ \begin{array}{c}                                     $	1
2.	Some fractions can be expressed as repeating decimals. Given that $\frac{1}{7} = 0.14285714285$ , what is the 9 <sup>th</sup> digit to the right of the decimal in the decimal representation of $\frac{3}{7}$ ?	2
3.	The two figures shown are made of unit squares. What is the positive difference of the perimeters, in units?	3
4.	If 9 wazzits can be purchased for \$1.80, what is the cost of 18 wazzits?	4
5.	What is the measure of angle 4 if $m \angle 1 = 76^\circ$ , $m \angle 2 = 27^\circ$ and $m \angle 3 = 17^\circ$ ?	5
6.	The graph of the equation $x + 2y + 3 = 0$ is perpendicular to the graph of the equation $ax + 2y + 3 = 0$ . What is the value of <i>a</i> ?	6
7.	A triangle has sides measuring 1 unit and 3 units. The length of the third side is an integer value of units. What is the length of the third side, in units?	7
8.	A worm has to climb a barrier 19 feet high. It climbs 8 feet every day and slips down 5 feet every night. Starting from the bottom of the barrier on Sunday morning, on which day of the week will the worm reach the top of the barrier?	8
9.	If $2x = 5y$ and $7y = 10z$ , what is the value of $\frac{z}{x}$ expressed as a common fraction?	9
10.	How many fifteen-minute appointments can a doctor fit into her schedule if she works from 8:30 am to noon and from 1 pm to 4:30 pm?	10
11.	If <i>j</i> and <i>k</i> are inversely proportional and $j = 16$ when $k = 21$ , what is the value of <i>j</i> when $k = 14$ ?	11
12.	What is 375% of $\frac{8}{30}$ ?	12

<ul><li>13. Each of the ten volumes of the collected works of Theodore Sturgeon is available in paperback for \$15 or in hardcover for \$25. Theresa buys a copy of each of the ten volumes for a total of \$220. How many hardcover volumes did she buy?</li></ul>	13
14. On a \$12.00 purchase, Michael was offered 3 successive discounts of 25%, 20% and 10% each in any order he wished. What is the difference in dollars between applying the discounts in order from greatest to least and in order from least to greatest?	14
15. "I weigh 40 pounds more than I did when I graduated from college," laments the math teacher. "I weigh 25% more now than I did then." How much did the math teacher weigh, in pounds, when he graduated from college?	15
16. Aaron has twice as many pencils as pens, and he has three more erasers than he has pens. He has eight pencils. How many erasers does he have?	16
17. The number 21 is the sum of two consecutive integers 10 and 11. What is the largest number of positive, consecutive integers whose sum is 21?	17
18. If $g(x) = x^2$ and $f(x) = 2x - 1$ , what is the value of $f(g(2))$ ?	18
19. At a state contest, 21 Mathletes stay in the same hotel. Each Mathlete gets his/her own room and the room numbers are 1 through 21. When all the Mathletes have arrived, except the ones staying in rooms 12 and 13, what is the median room number of the other 19 Mathletes?	19
20. A line goes through point A(9, 1), point B(19, <i>k</i> ) and point C(7, 0). What is the value of <i>k</i> ?	20
21. Given the equation $a + b = 30$ , where <i>a</i> and <i>b</i> are positive integers, how many distinct ordered-pair solutions $(a, b)$ exist?	21
22. For $y = \frac{1-x}{2x+3}$ and $x \neq -\frac{3}{2}$ , what is the value of y that is not attainable? Express your answer as a common fraction.	22
<ul><li>23. If the value of x is twice the value of y, what is the value of x<sup>2</sup> in terms of y?</li></ul>	23
24. The 3 <sup>rd</sup> and 5 <sup>th</sup> terms of an arithmetic sequence are 17 and 39, respectively. What is the 7 <sup>th</sup> term of the same sequence?	24

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25. In right triangle ABC, the length of side BC is 2 units, the length of side AC is 4 units and the measure of angle C is 60 degrees. What is the length of side AB, in units? Express your answer in simplest radical form.	25
26. Given the three digits 2, 4 and 7, how many different positive two- digit integers can be formed using these digits if a digit may not be repeated in an integer?	26
27. A triangle with sides measuring 8, 15 and 17 units is inscribed in a circle. What is the radius of the circle, in units? Express your answer as a decimal to the nearest tenth.	27
28. Quadrilateral ABCD is a parallelogram. If the measure of angle A is 62 degrees and the measure of angle ADB is 75 degrees, what is the measure of angle ADC, in degrees?	28
29. Anna Lisa bought two dozen apples for \$15.60. At that same rate, how much would three dozen of these apples cost?	29
30. How many different lines pass through at least two points in this 3-by-3 grid of lattice points shown?	30
31. A right triangle has legs measuring 20 inches and 21 inches. What is the length of the hypotenuse, in inches?	31
32. Danny Henry made a waffle on his six-inch-diameter circular griddle using batter containing a half a cup of flour. Using the same batter, and knowing that all waffles have the same thickness, how many cups of flour would Paul Bunyan need for his 24-foot-diameter circular griddle?	32
33. The functions $f(x) = x^2 - 2x + m$ and $g(x) = x^2 - 2x + 4m$ are evaluated when $x = 4$ . What is the value of <i>m</i> if $2f(4) = g(4)$ ?	33
34. In a factor tree, each value is the product of the two values below it, unless a value is a prime number already. What is the value of A on the factor tree shown? A $A = \frac{A}{3} + \frac{C}{2} + \frac{B}{3} + \frac{C}{2} + \frac{C}{2} + \frac{C}{2} + \frac{C}{3} + \frac$	34
35. The product of three consecutive integers is 120. That product divided by the mean of the three integers is 24. What is the largest of the three consecutive integers?	35
36. What is the area, in square inches, of a right triangle with a 24-inch leg and a 25-inch hypotenuse?	36
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37. The sum of the digits of a positive three-digit palindrome is equal to the square of the product of the digits. What is the palindrome?	37
38. Adam ran across the field at a speed of 5 yards per second and walked back along the same path at a speed of 2 yards per second. For how many seconds did he run if the total round-trip time was three and a half minutes?	38
39. The letters A, B and C are used to form every possible three letter "word." When these "words" are arranged in alphabetical order and numbered so that AAA is Word 1 and CCC is Word 27, what number will correspond to the position of word BAB on the list?	39
40. Leila is preparing boxed lunches for a group of 150 people. The lunches are the same except for the sandwiches. The four sandwich options are ham, turkey, roast beef or vegetarian. From past experience, she knows she will need 30% turkey, $\frac{1}{3}$ as many vegetarian as turkey and equal quantities of ham and roast beef. How many roast beef sandwiches will she make?	40
41. A triangle has side lengths measuring 30, 40 and 50 units. What is the length of its shortest altitude, in units?	41
42. A circle has an area of $\pi$ square units. What is the length of the circle's diameter, in units?	42
43. Place each of the digits 6, 7, 8 and 9 in exactly one square to make the smallest possible product. What is ×	43
44. A solid 6-by-6-by-6 cube is constructed from unit cubes and the entire outer surface is painted. What fraction of the unit cubes has at least two painted faces? Express your answer as a common fraction.	44
45. The product of two positive integers is 18. The positive difference of these two integers is 3. What is the sum of the two integers?	45
46. Two circles of radius 10 cm overlap such that each circle passes through the center of the other, as shown. How long, in cm, is the common chord (dotted segment) of the two circles? Express your answer in simplest radical form.	46
47. What is the greatest common divisor of all of the members of the set containing all numbers that are the product of four consecutive positive integers?	47
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48. A rhombus has sides of length 10 cm and one diagonal of length 12 cm. How long is the other diagonal, in cm?	48
49. If $\frac{x}{y} = 2$ and $\frac{z}{x} = 4$ , what is the value of $\frac{z}{y}$ ?	49
50. The Big Telescope Company sells circular mirrors. Their largest mirrors have radii of 5 meters and their smallest mirrors have radii of 1 meter. The cost of every mirror is proportional to the cube of the mirror's radius. What is the ratio of the total cost of 25 of the company's smallest mirrors to the cost of one of the company's largest mirrors? Express your answer as a common fraction.	50
51. What is the sum of all values of y for which the expression $\frac{y+6}{y^2-5y+4}$ is undefined?	51
52. What is the absolute value of the difference between the squares of 101 and 99?	52
53. When two fair six-faced dice are each rolled once, what is the probability that at least one of the numbers rolled is a 6? Express your answer as a common fraction.	53
54. A rectangle has a perimeter of 64 inches and each side has an integer length. How many non-congruent rectangles meet these criteria?	54
55. Two positive integers differ by 6 and their product is 135. What is the larger integer?	55
56. How much more is 25% of \$5 than 20% of \$2? Express your answer in terms of cents.	56
57. How many different four-letter arrangements can be formed using the six letters A, B, C, D, E and F, if the first letter must be C, one of the other letters must be B, and no letter can be used more than once in the arrangement?	57
58. When a rectangular wooden board is cut, the saw blade removes one-eighth of an inch of wood which becomes unused sawdust. A 5" by $x$ " board is cut 4 times perpendicular to the length and the result is a set of boards that are each 5" by 6.5". What is the value of $x$ ?	58
59. Henry drove along a straight highway at a constant speed of 60 miles per hour. He observed a pink car one-half mile behind him. The pink car was moving at an average speed that allowed it to pull up even with Henry in exactly three minutes. What was the pink car's average speed, in miles per hour?	59

60. A line through the points $(2, -9)$ and $(j, 17)$ is parallel to the line $2x + 3y = 21$ . What is the value of <i>j</i> ?	60
61. A set of five positive integers has a median of 3 and a mean of 11. What is the maximum possible value of the set's largest element?	61
62. What is the value of the expression $x^2 + 5x - 6$ , when $x = -1$ ?	62
63. The largest and smallest of three consecutive terms in an arithmetic sequence differ by 14. Half of the smallest term is added to each term and the sum of the resulting three numbers is 120. What is the value of the original smallest term?	63
64. Every day 10% of the liquid present in the morning in Kyle's open container will evaporate. At the end of three days, what percent of the original amount of liquid remains in Kyle's container? Express your answer to the nearest tenth.	64
65. An equilateral triangle and a square both have perimeters of 48 inches. What is the ratio of the length of the side of the triangle to the length of the side of the square? Express your answer as a common fraction.	65
66. The value of <i>x</i> is one-half the value of <i>y</i> , and the value of <i>y</i> is one-fifth the value of <i>z</i> . If <i>z</i> is 60, what is the value of <i>x</i> ?	66
67. In solving the system of equations $y = 7$ and $x^2 + y^2 = 100$ , what is the sum of the solutions for <i>x</i> ?	67
68. What is the measure of an angle, in degrees, if its supplement is six times its complement?	68
69. For positive integers <i>m</i> and <i>n</i> , how many integers are greater than the product <i>mn</i> and less than the product $(m + 1)(n + 1)$ ? Express your answer in terms of <i>m</i> and <i>n</i> .	69
70. Jamal needs three gallons of a mix that is two parts blue paint, three parts white paint and one part red paint. How many gallons of red paint will he need? Express your answer as a common fraction.	70
71. If x and y are numbers such that $(x + 3)(y - 5) = 0$ , what is the smallest possible value of $x^2 + y^2$ ?	71
72. An odd, three-digit positive integer has three distinct digits. The integer is a perfect cube, and the sum of its digits is also a perfect cube. What is the three-digit integer?	72

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73. There are two concentric spheres of radii 3 units and 6 units. What is the volume, in cubic units, of the region within the larger sphere and not within the smaller sphere? Express your answer in terms of $\pi$ .	73
74. What is the smallest two-digit positive integer such that the product of its two digits is one-half the integer?	74
75. What is the value of $(x - y)(x + y)$ if $x = 10$ and $y = 15$ ?	75
76. Define $a \ b$ to be $a(b+1) + ab$ . What is the value of $(-2) \ 3$ ?	76
77. What is 50% of $\frac{1}{3}$ of 36?	77
78. Carla rotated point A 420 degrees clockwise about point B and it landed at point C. Devon rotated the original point A $x$ degrees counterclockwise about point B and it also landed at point C. If $x < 360$ , what is the value of $x$ ?	78
79. The area of a particular square is <i>x</i> square units and its perimeter is <i>x</i> units. What is the value of <i>x</i> ?	79
80. A cubic block of wood with side lengths of 10 cm is cut into smaller cubes with side lengths of 1 cm. What is the ratio of the surface area of the larger block of wood to the combined surface area of the smaller blocks of wood? Express your answer as a common fraction.	80